

2002 Paper 5 Question 10

Foundations of Functional Programming

(a) Explain how a lambda-term can be converted into a form that uses only the combinators S and K. [4 marks]

(b) Illustrate your method by writing down a lambda term for each of the following functions and then expressing it in terms of just S and K.

(i) $\text{fun } I \ x = x$

(ii) $\text{fun } B \ f \ g \ x = f (g \ x)$

(iii) $\text{fun } C \ f \ x \ y = f \ y \ x$

(iv) $\text{fun } A \ x \ y = y (x \ x \ y)$

[4 marks each]